

LESSON 11 5 SQUARE ROOT FUNCTIONS ANSWERS

LESSON 11 5 SQUARE ROOT FUNCTIONS ANSWERS CAN BE AN ESSENTIAL TOPIC FOR STUDENTS TRYING TO MASTER ALGEBRA AND FUNCTIONS. UNDERSTANDING SQUARE ROOT FUNCTIONS IS A VITAL PART OF ALGEBRA THAT PROVIDES A FOUNDATION FOR MORE ADVANCED TOPICS IN MATHEMATICS. IN THIS ARTICLE, WE WILL EXPLORE THE CHARACTERISTICS OF SQUARE ROOT FUNCTIONS, HOW TO SOLVE THEM, AND PROVIDE ANSWERS TO VARIOUS PROBLEMS THAT YOU MAY ENCOUNTER IN LESSON 11 5.

UNDERSTANDING SQUARE ROOT FUNCTIONS

SQUARE ROOT FUNCTIONS ARE MATHEMATICAL FUNCTIONS THAT INVOLVE THE SQUARE ROOT OF A VARIABLE. THE GENERAL FORM OF A SQUARE ROOT FUNCTION CAN BE EXPRESSED AS:

$$f(x) = \sqrt{x}$$

THIS FUNCTION IS DEFINED FOR ALL $x \geq 0$ BECAUSE THE SQUARE ROOT OF A NEGATIVE NUMBER IS NOT A REAL NUMBER. THE GRAPH OF THIS FUNCTION IS A CURVE THAT STARTS AT THE ORIGIN $(0,0)$ AND INCREASES GRADUALLY AS x INCREASES.

CHARACTERISTICS OF SQUARE ROOT FUNCTIONS

SQUARE ROOT FUNCTIONS HAVE SEVERAL IMPORTANT CHARACTERISTICS:

1. DOMAIN: THE DOMAIN OF THE FUNCTION $f(x) = \sqrt{x}$ IS $[0, \infty)$, WHICH MEANS IT INCLUDES ALL NON-NEGATIVE REAL NUMBERS.
2. RANGE: THE RANGE IS ALSO $[0, \infty)$, AS THE OUTPUT OF THE FUNCTION IS ALWAYS NON-NEGATIVE.
3. INTERCEPTS: THE ONLY INTERCEPT IS AT THE ORIGIN $(0,0)$.
4. BEHAVIOR: AS x APPROACHES INFINITY, $f(x)$ ALSO APPROACHES INFINITY, BUT AT A DECREASING RATE. AS x APPROACHES ZERO, $f(x)$ APPROACHES ZERO.
5. SHAPE: THE GRAPH OF A SQUARE ROOT FUNCTION IS HALF OF A PARABOLA THAT OPENS TO THE RIGHT.

SOLVE SQUARE ROOT FUNCTIONS

WHEN SOLVING PROBLEMS INVOLVING SQUARE ROOT FUNCTIONS, IT IS CRUCIAL TO ISOLATE THE SQUARE ROOT ON ONE SIDE OF THE EQUATION. HERE ARE GENERAL STEPS TO SOLVE EQUATIONS THAT INVOLVE SQUARE ROOT FUNCTIONS:

1. ISOLATE THE SQUARE ROOT: MOVE ALL OTHER TERMS TO THE OPPOSITE SIDE.
2. SQUARE BOTH SIDES: THIS WILL ELIMINATE THE SQUARE ROOT BUT BE CAREFUL OF POTENTIAL EXTRANEIOUS SOLUTIONS.
3. SOLVE THE RESULTING EQUATION: THIS MAY REQUIRE ADDITIONAL ALGEBRAIC MANIPULATION.
4. CHECK YOUR SOLUTIONS: SUBSTITUTE BACK INTO THE ORIGINAL EQUATION TO ENSURE THEY ARE VALID.

COMMON PROBLEMS AND SOLUTIONS IN LESSON 11 5

IN LESSON 11 5, YOU MAY ENCOUNTER VARIOUS PROBLEMS INVOLVING SQUARE ROOT FUNCTIONS. BELOW ARE SOME TYPICAL PROBLEMS ALONG WITH THEIR SOLUTIONS.

PROBLEM 1: SOLVE THE EQUATION

$$\sqrt{x + 3} = 5$$

SOLUTION:

1. ISOLATE THE SQUARE ROOT:

$$\sqrt{x + 3} = 5$$

2. SQUARE BOTH SIDES:

$$x + 3 = 25$$

3. SOLVE FOR x :

$$x = 25 - 3$$

$$x = 22$$

4. CHECK THE SOLUTION:

$$\sqrt{22 + 3} = \sqrt{25} = 5 \text{ (VALID)}$$

ANSWER: $x = 22$

PROBLEM 2: SOLVE THE EQUATION

$$\sqrt{2x - 1} + 3 = 7$$

SOLUTION:

1. ISOLATE THE SQUARE ROOT:

$$\sqrt{2x - 1} = 4$$

2. SQUARE BOTH SIDES:

$$2x - 1 = 16$$

3. SOLVE FOR x :

$$2x = 16 + 1$$

$$2x = 17$$

$$x = \frac{17}{2} = 8.5$$

4. CHECK THE SOLUTION:

$$\sqrt{2(8.5) - 1} + 3 = \sqrt{17 - 1} + 3 = \sqrt{16} + 3 = 4 + 3 = 7 \text{ (VALID)}$$

ANSWER: $x = 8.5$

PROBLEM 3: SOLVE THE EQUATION

$$\sqrt{x^2 - 4} = x - 2$$

SOLUTION:

1. ISOLATE THE SQUARE ROOT:

$$\sqrt{x^2 - 4} = x - 2$$

2. SQUARE BOTH SIDES:

$$x^2 - 4 = (x - 2)^2$$

$$x^2 - 4 = x^2 - 4x + 4$$

3. REARRANGING GIVES:

$$0 = -4x + 8$$

$$4x = 8$$

$$\sqrt{x} = 2$$

4. CHECK THE SOLUTION:

$$\sqrt{\sqrt{2^2 - 4}} = \sqrt{4 - 4} = 0$$

$$\sqrt{2 - 2} = 0 \text{ (VALID)}$$

ANSWER: $x = 2$

SUMMARY OF KEY POINTS

UNDERSTANDING SQUARE ROOT FUNCTIONS AND THEIR PROPERTIES IS CRUCIAL FOR SOLVING ALGEBRAIC EQUATIONS. HERE'S A QUICK RECAP OF ESSENTIAL POINTS:

- SQUARE ROOT FUNCTIONS ARE DEFINED FOR NON-NEGATIVE VALUES.
- THE DOMAIN AND RANGE ARE BOTH $[0, \infty)$.
- SOLUTIONS TO SQUARE ROOT EQUATIONS REQUIRE CAREFUL MANIPULATION AND VERIFICATION.

PRACTICE PROBLEMS

TO FURTHER ENHANCE YOUR UNDERSTANDING, TRY SOLVING THESE PRACTICE PROBLEMS:

1. $\sqrt{3x + 5} = 8$

2. $\sqrt{5 - x} + 2 = 0$

3. $\sqrt{x^2 + 6} = x + 1$

BY CONSISTENTLY PRACTICING AND UNDERSTANDING SQUARE ROOT FUNCTIONS, YOU WILL GAIN CONFIDENCE IN SOLVING SIMILAR PROBLEMS IN LESSON 11.5 AND BEYOND.

FREQUENTLY ASKED QUESTIONS

WHAT ARE SQUARE ROOT FUNCTIONS?

SQUARE ROOT FUNCTIONS ARE MATHEMATICAL FUNCTIONS THAT INVOLVE THE SQUARE ROOT OF A VARIABLE, TYPICALLY EXPRESSED IN THE FORM $f(x) = \sqrt{x}$, WHERE x IS A NON-NEGATIVE REAL NUMBER.

HOW DO YOU GRAPH A SQUARE ROOT FUNCTION?

TO GRAPH A SQUARE ROOT FUNCTION, START BY PLOTTING POINTS FOR NON-NEGATIVE VALUES OF x . THE GRAPH WILL BEGIN AT THE ORIGIN $(0,0)$ AND INCREASE GRADUALLY, RESEMBLING HALF OF A SIDEWAYS PARABOLA.

WHAT IS THE DOMAIN OF THE SQUARE ROOT FUNCTION $f(x) = \sqrt{x}$?

THE DOMAIN OF THE SQUARE ROOT FUNCTION $f(x) = \sqrt{x}$ IS ALL NON-NEGATIVE REAL NUMBERS, OR $[0, \infty)$.

WHAT IS THE RANGE OF THE FUNCTION $f(x) = \sqrt{x}$?

THE RANGE OF THE FUNCTION $f(x) = \sqrt{x}$ IS ALSO ALL NON-NEGATIVE REAL NUMBERS, OR $[0, \infty)$.

WHAT TRANSFORMATIONS CAN BE APPLIED TO SQUARE ROOT FUNCTIONS?

TRANSFORMATIONS SUCH AS VERTICAL SHIFTS, HORIZONTAL SHIFTS, REFLECTIONS, AND STRETCHES/COMPRESSIONS CAN BE APPLIED TO SQUARE ROOT FUNCTIONS, ALTERING THEIR GRAPHS ACCORDINGLY.

HOW DO YOU SOLVE EQUATIONS INVOLVING SQUARE ROOT FUNCTIONS?

TO SOLVE EQUATIONS INVOLVING SQUARE ROOT FUNCTIONS, ISOLATE THE SQUARE ROOT ON ONE SIDE OF THE EQUATION AND THEN SQUARE BOTH SIDES TO ELIMINATE THE SQUARE ROOT, FOLLOWED BY SOLVING THE RESULTING EQUATION.

WHAT IS THE SIGNIFICANCE OF THE VERTEX IN A SQUARE ROOT FUNCTION?

IN A SQUARE ROOT FUNCTION, THE VERTEX REPRESENTS THE POINT WHERE THE GRAPH STARTS, TYPICALLY AT $(0,0)$ FOR THE BASIC FUNCTION $f(x) = \sqrt{x}$, AND IT INDICATES THE MINIMUM VALUE OF THE FUNCTION.

HOW DO YOU FIND THE INVERSE OF A SQUARE ROOT FUNCTION?

TO FIND THE INVERSE OF A SQUARE ROOT FUNCTION, SWAP THE X AND Y IN THE EQUATION AND SOLVE FOR Y. FOR EXAMPLE, THE INVERSE OF $f(x) = \sqrt{x}$ IS $f^{-1}(x) = x^2$.

WHAT ARE SOME REAL-WORLD APPLICATIONS OF SQUARE ROOT FUNCTIONS?

SQUARE ROOT FUNCTIONS CAN MODEL VARIOUS REAL-WORLD SCENARIOS, SUCH AS THE RELATIONSHIP BETWEEN DISTANCE AND AREA IN PHYSICS, GROWTH RATES IN BIOLOGY, AND FINANCIAL CALCULATIONS LIKE INTEREST RATES.

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